The “Physics” of Notations: Towards a Scientific Basis for Constructing Visual Notations in Software Engineering

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Abstract—Visual notations form an integral part of the language of software engineering (SE). Yet historically, SE researchers and notation designers have ignored or undervalued issues of visual representation. In evaluating and comparing notations, details of visual syntax are rarely discussed. In designing notations, the majority of effort is spent on semantics, with graphical conventions largely an afterthought. Typically no design rationale, scientific or otherwise, is provided for visual representation choices. While SE has developed mature methods for evaluating and designing semantics, it lacks equivalent methods for visual syntax. This paper defines a set of principles for designing cognitively effective visual notations: ones that are optimised for human understanding and problem solving. Together these form a design theory, called the Physics of Notations as it focuses on the physical (perceptual) properties of notations rather than their logical (semantic) properties. The principles were synthesised from theory and empirical evidence from a wide range of fields and rest on an explicit theory of how visual notations communicate. They can be used to evaluate, compare, and improve existing visual notations as well as to construct new ones. The paper identifies serious design flaws in some of the leading SE notations together with practical suggestions for improving them. It also showcases some examples of visual notation design excellence from SE and other fields.

Index Terms—modelling, analysis, diagrams, communication, visualization, visual syntax, concrete syntax

1. INTRODUCTION

Visual notations are pervasively used in software engineering (SE), and have dominated both research and practice since its earliest beginnings. The first SE visual notation was Goldstine and von Neumann’s program flow-charts, developed in the 1940s [36], and the ancestor of all modern SE visual notations [90]. This pattern continues to the present day with UML, the industry standard SE language, defined as “a visual language for visualising, specifying, constructing and documenting software intensive systems” [97]. Visual notations are used in all stages of the SE process, from requirements engineering through to maintenance. They play a particularly critical role in communicating with end users and customers, as they are believed to convey information more effectively to non-technical people than text [2].

Visual representations are effective because they tap into the capabilities of the powerful and highly parallel human visual system. We like receiving information in visual form and can process it very efficiently: around a quarter of our brains are devoted to vision, more than all our other senses combined [63]. In addition, diagrams can convey information more concisely [27] and precisely than ordinary language [8, 68]. Information represented visually is also more likely to be remembered due to the picture superiority effect [38, 70].

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“Very little is documented about why particular graphical conventions are used. Texts generally state what a particular symbol means without giving any rationale for the choice of symbols or saying why the symbol chosen is to be preferred to those already available. The reasons for choosing graphical conventions are generally shrouded in mystery.” [53]
ments (volumes), textual elements (labels) and spatial relationships. All of these elements can be used to construct the visual vocabulary of a notation (e.g. mind maps primarily consist of lines and labels). Graphical symbols are used to symbolise (or perceptually represent) semantic constructs, typically defined by a metamodel: the meanings of symbols are defined by mapping them to the constructs they represent. A valid expression in a visual notation is called a visual sentence or diagram. Diagrams consist of symbol instances (tokens), arranged according to the rules of the visual grammar.

Figure 1 summarises the scope of this paper. The paper says nothing about how to choose appropriate semantic constructs [139] or define their meaning [51], which are semantic issues: it only addresses how to visually represent a set of constructs when they have already been defined. It also says nothing about how to effectively represent diagrams [e.g. 29, 84], which are sentence level issues (though decisions made at the notation level strongly determine the effectiveness of diagrams that can be produced).

![Diagram](image)

Figure 1. Scope: this paper focuses on the top left hand quadrant of the diagram (visual syntax): it specifically excludes semantic issues (right hand side) and sentence-level issues (bottom).

1.2 The Dependent Variable: What Makes a “Good” Visual Notation?

The first problem that needs to be addressed in visual notation design is the lack of a clear design goal or dependent variable. To have any chance of success in a design task (or even to know if you have been successful), the endpoint must be clearly defined. Goals such as “simplicity”, “aesthetics”, “expressiveness”, and “naturalness” are often mentioned in the literature, but these are vaguely defined and highly subjective.

Visual notations are uniquely human-oriented representations: their sole purpose is to facilitate human communication and problem solving [50]. To be most effective in doing this, they need to be optimised for processing by the human mind. Cognitive effectiveness is defined as the speed, ease and accuracy with which a representation can be processed by the human mind [68]. This provides an operational definition of visual notation “goodness” that can be empirically evaluated. We propose this as the primary dependent variable for evaluating and comparing visual notations and the primary design goal in constructing them. Cognitive effectiveness determines the ability of visual notations to both communicate with business stakeholders and support design and problem solving by software engineers.

The cognitive effectiveness of visual notations is one of the most widely held (and infrequently challenged) assumptions in the IT field. However, cognitive effectiveness is not an intrinsic property of visual representations but something that must be designed into them [68]. Just putting information in graphical form does not guarantee that it will be worth a thousand of any set of words [21]. There can be huge differences between effective and ineffective diagrams and ineffective diagrams can be less effective than text.

1.3 Visual Syntax: An Important But Neglected Issue

Historically, SE researchers have ignored or undervalued the role of visual syntax. Notations tend to be evaluated based exclusively on their semantics, with issues of visual syntax rarely discussed [e.g. 98, 123]. When notations are empirically compared, differences are generally attributed to semantic rather than syntactic differences. For example, there have been many experimental studies comparing alternative notations for data modelling [e.g. 7, 121, 141]. All of these studies explain the empirical results in terms of their semantic differences, even though the differences in visual representation are just as great (if not greater). Visual representation thus acts as a significant (but unrecognised) confounding in most of these studies.

Visual Notation Design

Visual syntax is without question the “poor cousin” in notation design. Most effort is spent on designing semantics (what constructs to include and what they mean), with visual syntax (how to visually represent these constructs) largely an afterthought. For example, ArchiMate [67] is a language recently developed as an international standard for enterprise architecture modelling. The following quote clearly shows the subordinate role of visual syntax in designing the language:

“We do not put the notation of the ArchiMate language central but rather focus on the meaning of the language concepts and their relations. Of course, any modelling language needs a notation and we do supply a standard way of depicting the ArchiMate concepts but this is subordinate to the architectural semantics of the language.” [67]

Design rationale is the process of documenting design decisions made and the reasons they were made. This provides traceability in the design process and helps justify the final design [69]. Such rationale is conspicuously absent in design of SE visual notations: graphical conventions are typically defined without reference to theory or empirical evidence, or justifications of any kind [53]. When explanations are provided (which is rare), they tend to be based on common sense. For example, the following quote comes from one of the leading notation designers in the SE field (and one of the architects of UML):

“The selection of icons for any notation is a difficult task and not to be taken lightly. Indeed, icon design is largely an art not a science and requires a careful balance between expressiveness and simplicity. Our choice of the cloud icon suggests the boundaries of an abstraction, a concept that does not necessarily have plain or simple edges. The dashed lines indicate that clients generally only operate upon instances of a class, not the class itself.” [14]

Relying on common sense to make such decisions is unreliable, as the effects of graphic design choices are often counterintuitive [145]. However, even justifications of this kind are a great improvement on the usual situation where choice of symbols is not even discussed. A more common approach is to define symbols by assertion (e.g. “a class is represented by a rectangle”) or examples without any rationale at all. For example, UML does not provide design rationale for any of its graphical conventions [97], suggesting that this is acceptable practice even for the industry standard language.
The Problem of Visual Dialects

While SE has developed mature methods for evaluating semantics of notations, comparable methods for evaluating visual notations are notably absent. As a result, many SE notations exist in multiple visual forms or visual dialects. For example, two of the most successful notations in SE history are Data Flow Diagrams (DFDs) and ER Modelling. Both were developed in the 1970s but a recent survey shows they are the two most commonly used modelling techniques in practice [26]. Both of these notations exist in multiple visual forms. DFDs exist in two semantically equivalent dialects (Figure 2): the De Marco [27] dialect, consisting of circular “bubbles” and curved arrows and the Gane and Sarson [31] dialect, consisting of rounded rectangles (“rountangles” [50]) and right-angled lines.

Figure 2. Visual Dialects: De Marco DFDs vs Gane & Sarson DFDs. Same semantics, different visual syntax: which is best?

ER modelling also exists in a variety of visual dialects, with the Chen notation [18] the most commonly used in academic contexts and the Information Engineering (IE) notation [78] the most commonly used in practice. There are many other dialects associated with different CASE tools, development methodologies and research groups. Figure 3 shows the relationship conventions from some of the leading dialects.

Figure 3. Semantically equivalent forms of the ER Model. All these visual forms express the same underlying relationship semantics.

Despite the fact that these notations have been used in practice for over 30 years, there is still no consensus on which is best: neither market forces nor Darwinian-style selection mechanisms seem to be able to identify the “fittest” alternative. Without sound principles for evaluating and comparing visual notations, there is no reliable way to resolve such debates. As a result, the choice of an appropriate dialect normally comes down to personal taste.

1.4 Why Visual Representation is Important

The reason why visual notations have received so little attention is something of a mystery given their ubiquitous use in SE practice. One possible explanation is that researchers (especially those from mathematic backgrounds) see visual notations as being informal, and that serious analysis can only take place at the level of their semantics. However this is a misconception: visual languages are no less formal than textual ones [8, 51]. Another possible explanation is that methods for analysing visual representations are less mature than those for analysing verbal or mathematical representations [47, 75, 147] (which is something this paper aims to address). However, a third explanation is that SE researchers and notation designers simply consider visual syntax to be unimportant. While decisions about semantics (content) are treated with great care, decisions about visual representation (form) are often considered to be trivial or irrelevant: a matter of aesthetics rather than effectiveness [53].

This conventional wisdom is contradicted by research in diagrammatic reasoning, which shows that the form of representations has an equal, if not greater, influence on cognitive effectiveness as their content [68, 122, 151]. Human information processing is highly sensitive to the exact form information is presented to the senses: apparently minor changes in visual appearance can have dramatic impacts on understanding and problem solving performance [19, 68, 103, 122]. Empirical studies in SE have confirmed this: the visual form of notations significantly affects understanding, especially by novices [53, 56, 57, 79, 93, 106, 107]. This suggests that decisions about visual representation are far from trivial and should be treated with as much care (if not more) as decisions about semantics.

1.5 Objectives of this Paper

The use of visual notations in SE has a long history, from program flowcharts in the early days of computing (now largely extinct) to UML in the present. However, after more than half a century, the practice of designing SE visual notations lacks a scientific foundation. Currently, in evaluating, comparing and constructing visual notations we have little to go on but intuition and rule of thumb: we have neither theory nor a systematic body of empirical evidence to guide us.

This corresponds to what Alexander [1] calls an unconscious design culture: one that is not based on explicit design principles but on instinct, imitation and tradition. One characteristic of such cultures is that designers are unable to explain their designs. Another is a lack of variety of different forms: designers repeat the same patterns over and over again because they lack an understanding of the principles required to generate new ones. This may explain why SE visual notations look so similar to one another and change so little over time. For example, ER models as used in practice today look remarkably similar to Data Structure Diagrams, the first notation ever used to visualise database structures [3, 54]. Without knowledge of the underlying principles of graphic design, notation designers are unable to access the almost unlimited possibilities in the design space, and perpetuate the same (often flawed) ideas over time.

For visual notation design to progress from a “craft” to a design discipline (a selfconscious design culture), we need to define explicit principles for evaluating, comparing and constructing visual notations [1]. There is a wealth of theory and empirical evidence that could be used to produce such principles, though mainly outside the SE field. One reason for the lack of progress in establishing a science of visual notation design may be the strong NIH (Not Invented Here) effect in SE research, which draws on research from other fields to only a minimal extent (it has a self-referencing rate of 98.1% [34]).

The goal of this paper is to establish the foundations for a science of visual notation design. It defines a theory of how visual notations communicate (Section 3) and based on this, a set of principles for designing cognitively effective visual nota-

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1 As well as visual dialects (variants that exist in published form and used by a significant community of users), there are also countless colloquial forms (variants developed and used by particular individuals or organisations).
tions (Section 4). A secondary goal is to raise awareness about the importance of visual representation issues in notation design, which have historically received very little attention.

2. RELATED RESEARCH

2.1 Ontological Analysis

Ontological analysis has become widely accepted as a way of evaluating SE notations [33, 119]. The leading ontology used for this purpose is the Bunge-Wand-Weber (BWW) ontology, originally published in this journal [139]. Many ontological analyses have been conducted on different SE notations [e.g. 41, 98, 142]. Ontological analysis involves a two-way mapping between a modelling notation and an ontology. The interpretation mapping describes the mapping from the notation to the ontology while the representation mapping describes the inverse mapping [33]. According to the theory, there should be a one-to-one correspondence between the concepts in the ontology and constructs in the notation. If not, one or more of the following anomalies will occur (Figure 4):

- **Construct deficit** exists when there is no construct in the notation corresponding to a particular ontological concept.
- **Construct overload** exists when a single notation construct can represent multiple ontological concepts.
- **Construct redundancy** exists when multiple notation constructs can be used to represent a single ontological concept.
- **Construct excess** exists when a notation construct does not correspond to any ontological concept.

If construct deficit exists, the notation is said to be **ontologically incomplete**; if any of the other three anomalies exist, it is **ontologically unclear**. The BWW ontology predicts that ontologically clear and complete notations will be more effective. In Gregor’s taxonomy of theory types [45], this represents a **Type IV theory**: a theory for explaining and predicting. Extensive empirical research has been conducted to validate the predictions of the theory [e.g. 13, 117].

Ontological analysis provides a way of evaluating the semantics of notations but specifically excludes visual representation aspects: it focuses on content rather than form. If two notations have the same semantics but different syntax (e.g. Figure 2), ontological analysis cannot distinguish between them. Clearly, it would be desirable to have a comparable theory at the syntactic level so that visual syntax can also be evaluated in a sound manner.

2.2 Cognitive Dimensions of Notations (CDs)

Perhaps the closest thing to a theory of visual notation design that currently exists in the IT field is the Cognitive Dimensions of Notations (CDs) framework [10, 42, 44]. This has emerged as the predominant theoretical paradigm in visual languages (VLs) research. However, detailed analysis shows that it has serious theoretical and practical limitations for evaluating and designing visual notations [86]:

- It is not specifically focused on visual notations and only applies to them as a special case (as a particular class of cognitive artifacts) [43].
- The dimensions are vaguely defined, often leading to confusion or misinterpretation in applying them [25, 43].
- The theoretical and empirical foundations for the dimensions are poorly defined [43].
- The dimensions lack clear operationalisations (evaluation procedures or metrics), which means they can only be applied in a subjective manner [25, 43].
- It excludes visual representation issues, as it is based solely on structural properties [11].
- It does not support evaluation, as the dimensions simply define properties of notations and are not meant to be either “good” or “bad” [11, 44].
- It does not support design: the dimensions are not design guidelines and issues of effectiveness are excluded from its scope [11, 44].
- Its level of generality precludes specific predictions [11], meaning that it is **unfalsifiable**.

For all of these reasons, the CDs framework does not provide a scientific basis for evaluating and designing visual notations. In Gregor’s taxonomy [45], it represents a **Type I Theory**: a theory for analysing and describing. This is the earliest evolutionary form of theory and is appropriate when no prior theory exists. Such theories are traditionally regarded as unscientific as they lack testable propositions and cannot be falsified. However, they play a critical role in the development of any research field: for example, the pioneering work of the early taxonomists in biology paved the way for powerful Type IV theories like Darwin’s [45]. For this reason, a better term for such theories would be **prescientific**.

The CDs framework represents important pioneering work in advancing the analysis of visual notations beyond the level of intuition. But it should not be regarded as the end point for theory development in this field but as a starting point for developing a more powerful, domain-specific theory (the goal of this paper).

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2. Based on Popper’s criterion of falsifiability [105], the most widely accepted criterion for distinguishing between science and pseudoscience.
3. DESCRIPTIVE THEORY: HOW VISUAL NOTATIONS COMMUNICATE

This section defines a theory of how visual notations communicate based on extant theories from communication, semiotics, graphic design, visual perception and cognition. This defines a descriptive (positive) theory of visual notations, or in Gregor’s [45] terminology, a Type IV theory (a theory for explaining and predicting) (Figure 5). Only by understanding how and why visual notations communicate can we improve their ability to communicate: description provides the foundation for prescription.

3.1 Communication Theory

At the top level, the theory is an adaptation of Shannon and Weaver’s widely-accepted theory of communication [120] (or more precisely, a specialisation of this theory to the domain of visual notations). As shown in Figure 6, a diagram creator (sender) encodes information (message) in the form of a diagram (signal) and the diagram user (receiver) decodes this signal. The diagram is encoded using a visual notation (code), which defines a set of conventions that both sender and receiver understand. The medium (channel) is the physical form in which the diagram is presented (e.g. paper, whiteboard, computer screen). Noise represents random variation in the signal which can interfere with communication. The effectiveness of communication is measured by the match between the intended message and the received message (information transmitted). The work is widely considered to be for graphic design what the periodic table is for chemistry: the visual variables define a set of atomic building blocks that can be used to construct any visual representation, in the same way the periodic table can be used to construct any chemical compound. The visual variables thus define the dimensions of the graphic design space.

3.2 The Design Space (Encoding Side)

The seminal work in the graphic design field is Bertin’s *Semiology of Graphics* [8]. Bertin identified 8 visual variables that can be used to graphically encode information (Figure 7). These are divided into planar variables (the two spatial dimensions), and retinal variables (features of the retinal image). Bertin’s visual variables also define a set of primitives – a visual alphabet – for constructing visual notations: graphical symbols can be constructed by specifying particular values for visual variables (e.g. shape = rectangle, colour = green). Notation designers can create an unlimited number of graphical symbols by combining the variables together in different ways.

*Primary Notation, Secondary Notation and Noise*

Variations in visual variables convey meaning whether intended to or not. For example, size, colour and location of symbols have no formal meaning in UML class diagrams. However if these variables vary (intentionally or unintentionally), they will convey information over and above the literal meaning of the diagram. There are strong perceptual interpretations associated with such variations that are difficult to consciously override. Such variations play a similar role to non-verbal communication (e.g. facial expressions, tone of voice) in speech and can either reinforce or interfere with the intended meaning.

*Primary notation* refers to the formal definition of a visual notation: the set of graphical symbols and their prescribed (literal) meanings. *Secondary (informal) notation* refers to the use of visual variables not formally specified in the notation to reinforce or clarify meaning e.g. use of colour to highlight information. Secondary notation is not a trivial matter: Petre [103] found that effective use of secondary notation was the major distinguishing feature between expert and novice use of a notation. *Visual noise* (accidental secondary notation) refers to unintentional use or random variation in visual variables that conflicts with or distorts the intended message [47, 96].

3.3 The Solution Space (Decoding Side)

Newell and Simon [91] showed that human beings can be considered as information processing systems. Designing cognitively effective visual notations can therefore be seen as a problem of optimising them for processing by the human mind, in the same way that software systems are optimised for particular hardware. Principles of human graphical information processing provide the basis for making informed choices among the infinite possibilities in the design space.

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Footnote 3: Brightness is used instead of value (Bertin’s term) to avoid confusion with everyday usage of the word “value”. This variable defines a scale of relative lightness or darkness (black = 0 → white = 10).
Figure 8 shows a model of human graphical information processing, which reflects current research in visual perception and cognition. Processing is divided into two phases: perceptual processing (seeing) and cognitive processing (understanding). Perceptual processes are automatic, very fast and mostly executed in parallel while cognitive processes operate under conscious control of attention and are relatively slow, effortful and sequential. A major explanation for the cognitive advantages of diagrams is computational offloading: they shift some of the processing burden from the cognitive system to the perceptual system, which is faster and frees up scarce cognitive resources for other tasks. The extent to which diagrams exploit perceptual processing largely explains differences in their effectiveness [68, 103].

Figure 8. The Solution Space: maximising cognitive effectiveness means optimising notations for processing by the human mind

The stages in human graphical information processing are:

- **Perceptual discrimination**: features of the retinal image (colour, shape etc) are detected by specialised feature detectors [71, 130]. Based on this, the diagram is parsed into its constituent elements and separated from the background (figure-ground segregation) [100, 148].
- **Perceptual configuration**: structure and relationships among diagram elements are inferred based on their visual characteristics [100, 148]. The Gestalt Laws of Perceptual Organisation define how visual stimuli are organised into patterns or structures [144].
- **Attention management**: all or part of the perceptually processed image is brought into working memory under conscious control of attention. Perceptual precedence determines the order in which elements are attended to [65, 148].
- **Working memory**: this is a temporary storage area used for active processing, which reflects the current focus of attention. It has very limited capacity and duration and is a known bottleneck in visual information processing [64, 72].
- **Long term memory**: to be understood, information from the diagram must be integrated with prior knowledge stored in long term memory. This is a permanent storage area that has unlimited capacity and duration but is relatively slow [63]. Differences in prior knowledge (expert-novice differences) greatly affect speed and accuracy of processing.

4. **Prescriptive Theory: Principles for Designing Effective Visual Notations**

This section defines a set of principles for designing cognitively effective visual notations. These form a prescriptive theory for visual notations, or in Gregor’s [45] terminology, a Type V theory: a theory for design and action (Figure 5). Defining explicit principles transforms visual notation design from an unselfconscious process (craft) into a selfconscious process (design discipline).

The principles were developed using a best-evidence synthesis approach: they were synthesised from theory and empiri-
ontological analysis) (Figure 10):

- **Symbol redundancy** occurs when multiple graphical symbols can be used to represent the same semantic construct.
- **Symbol overload** occurs when two different constructs can be represented by the same graphical symbol.
- **Symbol excess** occurs when graphical symbols do not correspond to any semantic construct.
- **Symbol deficit** occurs when there are semantic constructs that are not represented by any graphical symbol.

This principle represents an extension of ontological analysis to the level of visual syntax, though its theoretical basis is in semiotics rather than ontology.

**Symbol redundancy**

Instances of symbol redundancy are called *synographs* (the equivalent of synonyms in textual languages). Symbol redundancy places a burden of choice on the notation user to decide which symbol to use and on the reader to remember multiple representations of the same construct. There are many instances of symbol redundancy in UML: Figure 11 shows an example of a construct synograph and a relationship synograph.

**Symbol overload**

Instances of symbol overload are called *homographs* (the visual equivalent of homonyms). This is the worst type of anomaly as it leads to ambiguity and the potential for misinterpretation [37]. It also violates one of the basic properties of the symbol system of graphics, *monosemy*, which means that each symbol should have a single meaning, defined in advance and independent of context [8]. ArchiMate violates this as the same graphical convention (spatial enclosure) can be used to show a range of different relationship types: inheritance, assignment, aggregation, composition and grouping (Figure 12).

**Symbol excess**

Symbol excess adds to diagrammatic complexity (Complexity Management) and graphic complexity (Graphic Economy), which both adversely affect understanding [93]. UML includes several instances of symbol excess, the most obvious being the ubiquitous *comment*, which can appear on all diagram types (Figure 13). These are used to clarify meaning of diagrams and perform a similar role to comments in programs. Including textual explanations on diagrams is a useful practice, but it is neither necessary nor desirable to show them using explicit symbols: this is an example of what graphic designers call “boxitis” [131, 132, 146]. Such symbols add visual clutter to diagrams and confound their interpretation by making it more likely they will be interpreted as constructs. A simple block of text would be less intrusive and less likely to be misinterpreted.

**Symbol deficit**

In most SE contexts, symbol deficit is desirable to limit diagrammatic complexity (Complexity Management) and graphic complexity (Graphic Economy). Given the semantic complexity of most SE notations, it is usually counterproductive to try to show all constructs on the diagram. This represents a clear difference with ontological analysis where all deviations from a 1:1 mapping are considered harmful [33].

4.2 Principle of Perceptual Discriminability: Different symbols should be clearly distinguishable from each other

**Perceptual discriminability** is the ease and accuracy with which graphical symbols can be differentiated from each other. This relates to the first phase of human visual information processing: perceptual discrimination (Figure 8). Accurate discrimination between symbols is a prerequisite for accurate interpretation of diagrams [147].

**Visual Distance**

Discriminability is primarily determined by the *visual distance* between symbols. This is measured by the number of visual variables on which they differ and the size of these differences (measured by the number of perceptible steps). Each visual variable has an infinite number of physical variations but only a finite number of perceptible steps (values that are reliably discriminable by the human mind) [8]. Research in psychophysics has established *discriminability thresholds* for most visual variables, which can be used to guide choice of values [8, 125, 126]. In general, the greater the visual distance between symbols, the faster and more accurately they will be recognised [148]. If differences are too subtle, errors in interpretation may result. Requirements for discriminability are higher for novices than for experts as we are able to make much finer distinctions with experience [15].

Many SE notations have very poor discriminability, as they consist of shapes and connecting lines that are too similar. For example, experimental studies show that entities and relation-
ships are often confused by novices on ER diagrams (Figure 14) [93]. The visual distance between the symbols is relatively small, as they differ on only one visual variable (shape) and the shapes belong to the same family (quadrilaterals).

Figure 14. Experimental studies show that rectangles and diamonds in ER diagrams are frequently confused by novices

The Primacy of Shape

Of all visual variables, shape plays a special role in discriminating between symbols as it represents the primary basis on which we identify objects in the real world. In fact, theories of object recognition differ only to the extent that they consider object representations to be based only on shape or if other features are also involved [9, 77, 113]. For this reason, shape should be used as the primary visual variable for distinguishing between different semantic constructs. For example, discriminability of ER diagrams could be improved by using shapes from different families (Figure 15). It is surprising that after more than 3 decades of use and the empirically-established confusion between them that such a change has not been made already.

Figure 15. Entities and relationships could be made more discriminable by using shapes from different families

Most SE notations use a perceptually limited repertoire of shapes, mostly rectangle variants [103]. This is surprising as shape has the largest range of values (capacity) of any visual variable and it is the only visual variable used in most SE notations (see Visual Expressiveness). As an example of design excellence, De Marco-style DFDs use clearly discriminable shapes to represent different constructs: all come from different families (Figure 16). In contrast, the Gane and Sarson dialect uses rectangle variants for all constructs (Figure 16).

Figure 16. Graphic excellence vs graphic mediocrity: De Marco DFDs (top) use clearly distinguishable shapes for all constructs while Gane and Sarson DFDs (bottom) use rectangle variants.

Redundant Coding

Redundancy is an important technique in communication theory to reduce errors and counteract noise [40, 120]. The visual distance between symbols can be increased by redundant coding: using multiple visual variables to distinguish between them [72]. As an example, colour could be used to improve discriminability between entities and relationships in ER diagrams (Figure 17). Most SE diagramming notations rely on only a single variable to distinguish between symbols, which is less robust to misinterpretation.

Figure 17. Redundant Coding: using multiple visual variables (shape + colour) to distinguish between symbols

Perceptual Popout

According to feature integration theory, visual elements with unique values for at least one visual variable can be detected pre-attentively and in parallel across the visual field [108, 130]. Such elements appear to “pop out” from a display without conscious effort. On the other hand, visual elements that are differentiated by unique combinations of values (conjunctions) require serial search, which is much slower and error-prone.

The clear implication of this for visual notation design is that each graphical symbol should have a unique value on at least one visual variable. This requirement is violated in UML Class Diagrams, where 3 visual variables (shape, brightness, texture) are used in combinatorial fashion to distinguish between 20 different types of relationships (Table 1). Discrimination between relationship types relies on unique combinations of values, sometimes in combination with labels or context. Only two of the relationship types have unique values on any variable, which precludes perceptual popout in most cases.

Table 1. Relationship Types on UML Class Diagrams

<table>
<thead>
<tr>
<th>Aggregation</th>
<th>Association (navigable)</th>
<th>Association (non-navigable)</th>
<th>Association class relationship</th>
<th>Composition</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Constraint</td>
<td>Dependency</td>
<td>Generalisation</td>
<td>Generalisation set</td>
<td>Interface (provided)</td>
</tr>
<tr>
<td>Interface (required)</td>
<td>N-ary association</td>
<td>Note reference</td>
<td>Package containment</td>
<td>Package import (public)</td>
</tr>
<tr>
<td>Package import (private)</td>
<td>Package merge</td>
<td>Realisation</td>
<td>Substitution</td>
<td>Usage</td>
</tr>
</tbody>
</table>

Note that redundant coding is different to using conjunctions to distinguish between symbols. Conjunctions use visual variables in a multiplicative (combinatorial) manner: each variable is necessary but not sufficient to distinguish between symbols (only combinations of values are unique). In redundant coding, variables are used in an additive (reinforcing) manner: each variable is sufficient on its own to distinguish between symbols. For example, in Figure 17, each symbol has a unique value for each variable (shape and colour), so in principle either could be used to distinguish between them.

Textual Differentiation

SE notations sometimes rely on text to distinguish between symbols. For example, UML frequently uses text and typographic characteristics (bold, italics, underlining) to distinguish between element and relationship types (Figure 18), [149], one of the leading requirements engineering notations, uses

4 This was more a matter of good luck than good design as the phenomenon of perceptual popout was only discovered after DFDs were designed.
labels to differentiate between most of its relationship types [87]. Symbols that differ only on textual characteristics are technically homographs, as they have zero visual distance (Semantic Clarity).

Textual differentiation of symbols is a common but cognitively inefficient way of dealing with excessive graphic complexity (Graphic Economy) as text processing relies on less efficient cognitive processes. To maximise discriminability, symbols should be differentiated using visual variables, so that differences can be detected automatically and in parallel by the perceptual system. Textual differentiation of symbols also confounds the role of text in diagrams. Labels play a critical role at the sentence (diagram) level, in distinguishing between symbol instances (tokens) and defining their correspondence to the real world domain. For example, with the labels in Figure 17, the two entity types would be indistinguishable and the diagram would lack real world meaning. Using labels to distinguish between symbol types (at the language level) confounds their role. Also, when labels are used to distinguish between relationship types (Figure 18), it precludes the use of user-defined and domain-relevant names. Text is an effective way to distinguish between symbol instances but not between symbol types.

4.3 Principle of Semantic Transparency: Use visual representations whose appearance suggests their meaning

Semantic transparency is defined as the extent to which the meaning of a symbol can be inferred from its appearance. While Perceptual Discriminability simply requires that symbols should be different from each other, this principle requires that they provide cues to their meaning (form implies content). The concept of semantic transparency formalises informal notions of “naturalness” or “intuitiveness” that are often used when discussing visual notations, as it can be evaluated experimentally. Semantically transparent representations reduce cognitive load because they have built-in mnemonics: their meaning can be either perceived directly or easily learnt [103]. Semantic transparency is not a binary state but a continuum (Figure 19):

- A symbol is semantically immediate if a novice reader would be able to infer its meaning from its appearance alone (e.g. a stick figure to represent a person).
- A symbol is semantically opaque (or conventional) if there is a purely arbitrary relationship between its appearance and its meaning (e.g. rectangles in ER diagrams): this represents the zero point on the scale.
- A symbol is semantically perverse (or a false mnemonic), if a novice reader would be likely to infer a different (or even opposite) meaning from its appearance: this represents a negative value on the scale. Some UML conventions (e.g. package merge) have this unfortunate property.
- In between semantic immediacy and opacity there are varying degrees of semantic trans lucency (or mnemonic ity), where symbols provide a cue to their meaning (and therefore an aid to memory) but require some initial explanation.

The most obvious form of association between symbols and their referent concepts is perceptual resemblance, but many others are also possible: common logical properties (e.g. spatial inclusion in Venn diagrams), functional similarities (e.g. trash can for deleted items), metaphor (e.g. crossed swords for conflict) and cultural associations (e.g. red for danger). Semantic transparency corresponds to Norman’s [94] concept of natural mappings: using physical analogies, visual metaphors and cultural associations to design objects. It also corresponds to Gurr’s concept of systematicity: matching semantic properties of represented objects to visual properties of symbols [47].

Icons (perceptual resemblance)

Icons are symbols that perceptually resemble the concepts they represent [102]. This reflects a basic distinction in semiotics, between symbolic and iconic signs [102]. Iconic representations speed up recognition and recall and improve intelligibility of diagrams to naïve users [15, 79]. They also make diagrams more accessible to novices: a representation composed of pictures appears less daunting than one composed of abstract symbols [103]. Finally, they make diagrams more visually appealing: people prefer real objects to abstract shapes [5, 103].

Icons are pervasively used in HCI (e.g. graphical user interfaces) [92] and cartography [111] but surprisingly rarely in SE visual notations. Most SE notations rely exclusively on abstract geometrical shapes to represent constructs [103]. Such symbols don’t convey anything about their referent concepts: their meaning is purely conventional and must be learnt. Rich pictures [17] are a rare example of an SE visual notation that is almost exclusively iconic: the resulting diagrams are visually appealing and cartoon-like, unlike the dull, technical-looking diagrams typically used in SE practice (Figure 20).
**Semantically Transparent Relationships**

Semantic transparency also applies to representing relationships. Certain spatial arrangements of visual elements predispose people towards a particular interpretation of the relationship among them even before the meaning of the elements is known [47, 147]. In a set of experiments designed to discover how diagrams are spontaneously interpreted, Winn [147] used diagram elements with nonsense labels arranged in different spatial configurations and asked subjects to describe the relationships among them. The results are summarised in Figure 21.

![Figure 21. Semantically transparent relationships: these spatial relationships are interpreted in a spontaneous or natural way [147]](image)

Most SE visual notations make only limited use of such relationships and rely mainly on different types of connecting lines to represent relationships (e.g. Table 1). Such links are very versatile but provide few clues to their meaning as they can be used to represent almost any type of relationship. Figure 22 shows how spatial relationships (spatial enclosure and overlap) could be used to represent overlapping subtypes in ER models. This conveys the relationship among the entities in a more semantically transparent way than using arrows, so is more likely to be interpreted correctly and more easily remembered.

![Figure 22. Spatial enclosure and overlap (right) convey the concept of overlapping subtypes in a more semantically transparent way than arrows (left).](image)

The representation on the right of Figure 22 obeys the principle of systemacity [47] as spatial enclosure has the same logical properties as the IS-A (subtype) relationship: transitivity, irreflexivity and asymmetry. The extent to which diagrams exploit such mappings can greatly improve their effectiveness for problem solving [19, 47, 68, 114]. It also prevents errors in using the notation, as the geometric properties of the spatial relationship enforce the logical constraints on the relationship [20, 114]. It also makes subtype relationships more discriminable from all other types of relationships (Perceptual Discriminability).

Note that spatial enclosure could not be used to represent generalisation in UML. Firstly, spatial enclosure is already used for many other purposes in UML, so would lead to symbol overload (Semiotic Clarity). Secondly, it would violate the principle of systemacity. UML supports multiple inheritance, which allows many-to-many relationships between superclasses and subclasses. This conflicts with the geometric properties of spatial enclosure, which allows only one-to-many relationships.

4.4 Principle of Complexity Management: Include explicit mechanisms for dealing with complexity

Complexity management refers to the ability of a visual notation to represent information without overloading the human mind. Complexity is also one of the defining characteristics of the SE field, where complexity levels exceed those in any other discipline [28, 32]. It is also one of the most intractable problems in visual notation design: a well-known problem with visual representations is that they do not scale well [22]. Currently, complexity management is incorporated into SE visual notations in notation-specific ways (point solutions [16]) or not at all: this principle defines general requirements for a solution to complexity management in visual notations.

In this context, “complexity” refers to diagrammatic complexity, which is measured by the number of elements (symbol instances or tokens) on a diagram. While this is ostensibly a diagram (sentence) level issue, it requires notation-level features to solve it. Complexity has a major effect on cognitive effectiveness as the amount of information that can be effectively conveyed by a single diagram is limited by human perceptual and cognitive abilities:

- **Perceptual limits:** The ability to discriminate between diagram elements increases with diagram size [101].
- **Cognitive limits:** The number of diagram elements that can be comprehended at a time is limited by working-memory capacity. When this is exceeded, a state of cognitive overload ensues and comprehension degrades rapidly [82].

Effective complexity management is especially important when dealing with novices, who are less equipped to cope with complexity [127]. Excessive complexity is one of the major barriers to end user understanding of SE diagrams [83, 118].

Surprisingly, some of the leading SE visual notations lack mechanisms for managing complexity. In the absence of these, problems must be represented as single monolithic diagrams, no matter how complex they become. For example, the ER model has been used for over 3 decades and still lacks such mechanisms. As a result, “absurdly complex diagrams” are often produced in practice that overwhelm end users [61] (see Figure 23 for a real world example). A language developed more recently and specifically for communication with end users, also lacks such mechanisms [87], showing that this lesson has still not been learnt over time.

![Figure 23. In the absence of complexity management mechanisms, ER models must be shown as single monolithic diagrams.](image)

---

6 This should be clearly distinguished from graphic complexity, which measures the number of symbol types in a notation (Graphic Economy).
In the absence of explicit complexity management mechanisms, practitioners often develop informal solutions to the problem, meaning that it is solved by secondary notation. However, this is undesirable as it results in highly idiosyncratic solutions and proliferation of colloquial forms. According to ontological theory [142], complexity management mechanisms are essential elements of all SE notations, which means they should be included in the primary notation.

To effectively represent complex situations, visual notations must provide mechanisms for modularisation and hierarchically structuring; these correspond to subsystems and level structures in ontological theory [142]. However, while ontological theory defines the semantic constructs required to support complexity management, it does not define a syntactic solution to the problem.

Modularisation

The most common way of reducing complexity of large systems is to divide them into smaller parts or subsystems: this is called modularisation. Baldwin and Clark [4] have proposed this as a unifying paradigm for the IT industry, which helps cope with the mind-boggling levels of complexity encountered. To avoid overloading the human mind, notations must provide the ability to divide large diagrams into perceptually and cognitively manageable “chunks”. Cognitive load theory shows that reducing the amount of information presented at a time to within the limitations of working memory improves speed and accuracy of understanding and facilitates deep understanding of information content [80, 127]. Empirical studies show that modularising SE diagrams can improve end user understanding and verification by more than 50% [83]. Modularisation can take place in a top down (e.g. decomposition à la DFDs) or bottom up manner (e.g. packages in UML).

Modularisation requires certain semantic constructs to be included in the notation: either a subsystem construct (e.g. UML packages) or decomposable constructs (e.g. UML activities). But including such constructs is not enough: for this to be effective at the syntactic level, diagrammatic conventions for decomposing diagrams need to be defined. In particular, UML packages provide a semantic but not a syntactic solution to the problem of complexity management (which requires more than defining a graphical symbol to represent the construct).

Hierarchy (levels of abstraction)

Hierarchy is one of the most effective ways of organising complexity for human comprehension as it allows systems to be represented at different levels of detail, with complexity manageable at each level [30]. This supports top down understanding, which has been shown to improve understanding of SE diagrams [93]. Simon [124] proposed hierarchy as a general architecture for structuring complex systems.

Hierarchical organisation is a natural result of top-down decomposition: when a system is decomposed to multiple levels, the result will usually be a hierarchy of diagrams at different levels of abstraction. When modularisation takes place in a bottom up manner, higher level diagrams need to be explicitly created by a process of summarisation (abstraction). Elements on higher level diagrams “explode” to complete diagrams at the next level, following the principle of recursive decomposition [27] (Figure 24). This simple mechanism supports both modularisation and hierarchical structuring and is the common denominator among visual notations that effectively manage complexity (e.g. UML Activity Diagrams, Statecharts). Visual languages that support recursive decomposition are called hierarchical visual languages [24].

![Hierarchical organisation](image)

Figure 24. Hierarchical organisation allows a system to be represented at multiple levels of abstraction, with complexity manageable at each level.

An example of excellence in managing diagrammatic complexity in the SE field (and probably one of the best examples in any field) are DFDs. These incorporate modularity, hierarchical structuring and an explicit complexity limit: 7 ± 2 “bubbles” per diagram (consistent with the known limits of working memory). In this respect, they were ahead of their time, and still are: many more recent SE notations could learn from their example. In particular, UML lacks a consistent approach to complexity management: different diagram types have different ways of dealing with complexity, while some diagram types (e.g. class diagrams) have none at all.

4.5 Principle of Cognitive Integration: Include explicit mechanisms to support integration of information from different diagrams

Cognitive integration only applies when multiple diagrams are used to represent a system. This is a critical issue in SE, where problems are typically represented by systems of diagrams rather than single diagrams. It applies equally to diagrams of the same type (homogeneous integration) – for example, a set of levelled DFDs – or diagrams of different types (heterogeneous integration) – for example, a suite of UML diagrams or ArchiMate views. This principle is closely related to Complexity Management, which leads to multiple diagrams as a result of modularisation, but applies even when modularity is not used (due to heterogeneous integration).

Representing systems using multiple diagrams places additional cognitive demands on the reader to mentally integrate information from different diagrams and keep track of where they are [122]. Kim et al [48, 60] have proposed a theory to address this issue, called the cognitive integration of diagrams. This is an important contribution, as most previous research in diagrammatic reasoning has focused on single diagrams. According to their theory (which has been validated in an SE context), for multi-diagram representations to be cognitively effective, they must include explicit mechanisms to support (Figure 25):

- Conceptual integration: mechanisms to help the reader assemble information from separate diagrams into a coherent mental representation of the system.
• **Perceptual integration**: perceptual cues to simplify navigation and transitions between diagrams.

![Diagram](image1)

**Figure 25. Cognitive Integration**: When multiple diagrams are used to represent a domain, explicit mechanisms are needed to support perceptual and conceptual integration.

**Conceptual Integration**

One important mechanism to support conceptual integration is a **summary (longshot) diagram**, which provides a view of the system as a whole. This acts as an overall cognitive map into which information from individual diagrams can be assembled [60, 109]. Examples of such diagrams are **rich pictures** in Soft System Methodology and **context diagrams** in DFDs. In homogeneous integration, such a diagram is a natural result of hierarchical structuring: it is the “root” of the hierarchy. However in heterogeneous integration, a new diagram will need to be created for this purpose.

**Contextualisation** (or focus + context) is a technique used in information visualisation where the part of a system of current interest (focus) is displayed in the context of the system as a whole [66, 134]. In a diagramming context, this means including contextual information on each diagram showing its relationships to elements on other diagrams. The simplest and most effective way to do this is to include all directly related elements from other diagrams (its “immediate neighbourhood”) as **foreign elements** (Figure 26). Including overlap between diagrams in this way allows each element in the system of diagrams to be understood in terms of its relationships to all other elements, which supports conceptual integration. It also supports perceptual integration by simplifying transitions between related diagrams, through the mechanism of **visual momentum** [140].

![Diagram](image2)

**Figure 26. Contextualisation**: each diagram should include its surrounding context to show how it fits into the system as a whole.

**Perceptual Integration**

There are a range of mechanisms that can be used to support perceptual integration, which draw on the design of physical spaces (urban planning), virtual spaces (HCI) and graphical spaces (cartography and information visualisation). Whether navigating around a city, a website, an atlas, or a set of diagrams, **wayfinding** follows the same four stages [74]:

- Orientation: where am I?
- Route choice: where can I go
- Route monitoring: am I on the right path?
- Destination recognition: am I there yet?

Clear labelling of diagrams **(identification)** supports orientation and destination recognition. **Level numbering** (as used to show structure of documents) supports orientation by showing the user where they are in the system of diagrams. Including **navigational cues** on diagrams **(signposting)** supports route choice. A **navigational map**, showing all diagrams and the navigation paths between them, supports orientation, route monitoring and route choice: readers can use this to navigate through the information space and keep track of where they are.

No existing notations fully satisfy this principle (which is not surprising as the theory is relatively new), but DFDs come closest: they include a longshot diagram **(context diagram)**, orientation information **(level numbering)** and contextualisation **(balancing)**. However, they lack a navigational map, don’t support horizontal (lateral) navigation, and downward navigation is ambiguous. UML is a counter-exemplar as it lacks a longshot diagram and the relationships between different diagram types are unclear.

### 4.6 Principle of Visual Expressiveness: Use the full range and capacities of visual variables

**Visual expressiveness** is defined as the number of visual variables used in a notation. This measures utilisation of the graphic design space. While **visual distance** (Perceptual Discriminability) measures pair-wise visual variation between symbols, visual expressiveness measures visual variation across the entire visual vocabulary. Using a range of visual variables results in a perceptually enriched representation that exploits multiple visual communication channels and maximises computational offloading.

Visual expressiveness partitions the set of visual variables into two subsets (Figure 27):

- **Information-carrying variables**: variables used to encode information in a notation.
- **Free variables**: variables not (formally) used.

The number of free variables is called the **degrees of visual freedom** and is the inverse of visual expressiveness. A notation with no information-carrying visual variables (visual expressiveness = zero; eight degrees of visual freedom) is called **non-visual** (or textual), while a notation that uses all visual variables (visual expressiveness = eight; zero degrees of visual freedom) is **visually saturated**.

![Diagram](image3)

**Figure 27. Visual Expressiveness**

Most SE notations use only a single visual variable to encode information: shape (see Figure 28). Such notations are **visually one-dimensional**: they use only one of the eight available visual communication channels, and ironically, the one with the lowest bandwidth. Shape is one of the least powerful visual
variables as it can only be used to encode nominal data and is one of the least cognitively efficient [73].

In contrast to the visually impoverished forms of SE notations, Figure 29 shows an example from cartography, a discipline with over 5,000 years experience in graphically encoding information. This defines 38 different graphical conventions using 6 visual variables (shape, texture, brightness, size, colour, orientation). This is an order of magnitude more visually expressive than most SE notations and represents the point of visual saturation in cartography (as the planar variables are reserved for encoding geographical location).

A second point to note about this example is that 5 visual variables (shape, texture, brightness, size, colour) are used to distinguish between 19 types of lines with no conjunctions. Compare this to Table 1, which uses 3 visual variables to distinguish between a similar number of lines with mostly conjunctions. This shows how visual expressiveness can be used to improve discriminability (Perceptual Discriminability). Cartographers are masters of graphical representation and notation designers can learn much from them.

**Use of Colour**

Colour is one of the most cognitively effective of all visual variables; the human visual system is highly sensitive to variations in colour and can quickly and accurately distinguish between them [76, 148]. Differences in colour are detected three times faster than shape and are also more easily remembered [71, 128]. Yet surprisingly, colour is rarely used in SE notations and is specifically prohibited in UML:

"UML avoids the use of graphic markers, such as colour, that present challenges for certain persons (the colour blind) and for important kinds of equipment (such as printers, copiers, and fax machines)." [97]

Archimate is an example of graphic excellence in this respect, as it uses colour to distinguish between concepts in different architectural layers (Figure 30). This enables information in different architectural layers to be separated in the mind [19].

**Choice of visual variables: form follows content**

The choice of visual variables should not be arbitrary but should be based on the nature of the information to be conveyed [8]. Different visual variables have properties that make them suitable for encoding different types of information. For example, colour can only be used for nominal data as it is not psychologically ordered [64]. Also, different visual variables have different capacities (number of perceptible steps) [8, 126]. The properties of each visual variable have been established by research in psychophysics (summarised in Table 2).

![Table 2](image)

<table>
<thead>
<tr>
<th>Variable</th>
<th>Power</th>
<th>Capacity</th>
</tr>
</thead>
<tbody>
<tr>
<td>Horizontal position (x)</td>
<td>Interval 10-15</td>
<td></td>
</tr>
<tr>
<td>Vertical position (y)</td>
<td>Interval 10-15</td>
<td></td>
</tr>
<tr>
<td>Size</td>
<td>Interval 20</td>
<td></td>
</tr>
<tr>
<td>Brightness</td>
<td>Ordinal 6-7</td>
<td></td>
</tr>
<tr>
<td>Colour</td>
<td>Nominal 7-10</td>
<td></td>
</tr>
<tr>
<td>Texture</td>
<td>Nominal 2-5</td>
<td></td>
</tr>
<tr>
<td>Shape</td>
<td>Nominal Unlimited</td>
<td></td>
</tr>
<tr>
<td>Orientation</td>
<td>Nominal 4</td>
<td></td>
</tr>
</tbody>
</table>

The aim should be to match properties of visual variables to the properties of the information to be represented (i.e. form follows content):
• Power: the power of the visual variable should be greater than or equal to the measurement level of the information.
• Capacity: the capacity of the visual variable should be greater than or equal to the number of values required.

**SE notations use only a limited range of values of visual variables**

As well as using only a limited range of the visual variables available, SE notations also use only a limited range of the possible values of each variable (capacity). For example, they use a very limited repertoire of shapes, mostly rectangle variants [103]. These are the least effective shapes for human visual processing and empirical studies show that curved, 3-dimensional and iconic shapes should be preferred [5, 56, 147]. Other visual variables are used in binary fashion: for example, UML uses brightness and texture in addition to shape but only two values of each: black and white for value; solid and dashed for texture. The combination of using only a small subset of visual variables and a small subset of the capacity of each variable means that SE notations utilise only a tiny fraction of the graphic design space.

**Textual vs graphical encoding**

To maximise visual expressiveness, graphical encoding should be preferred to textual encoding (subject to constraints on graphic complexity: see Graphic Economy). The more work that can be done by visual variables, the greater the role of perceptual processing and computational offloading. To illustrate possible tradeoffs between visual and textual encoding in notation design, Figure 31 shows three alternative encodings of relationship cardinalities (or multiplicities). These represent three different levels of visual expressiveness:

- 0: the UML convention, which is non-visual (i.e. textual)
- 1: the IE convention, which uses shape
- 2: the Oracle convention, which uses shape (to encode the maximum) and texture (to encode the minimum)

The UML convention is the most semantically expressive as it can define exact values for minimum and maximum cardinalities (rather than 0, 1 or many like the other two). However, it is the least cognitively effective as it relies entirely on text processing [57]. The IE and Oracle representations are also more semantically transparent as the multiple claws of the “crow’s foot” suggests a many relationship: the effectiveness of this has been confirmed by experimental studies [e.g. 57, 107].

![Figure 31. Levels of Visual Expressiveness: UML (left) = 0; IE (middle) = 1 (shape); Oracle (right) = 2 (shape, brightness).](image)

The UML convention is therefore less discriminable, less semantically transparent and less visually expressive than the other two, so represents a poor compromise between semantic expressiveness and cognitive effectiveness (though a fairly typical one, as SE notation designers tend to prioritise semantic expressiveness over everything else). Surprisingly, UML was developed more recently than the other two techniques, so represents a later “evolutionary form”. However, without sound theory and principles for choosing between alternative representations, notations can get worse rather than better over time.

**4.7 Principle of Dual Coding: Use text to complement graphics**

Perceptual Discriminability and Visual Expressiveness both advise against using text to encode information in visual notations. However, this does not mean that text has no place in visual notation design. Pictures and words are not enemies and should not be mutually exclusive [39, 131]. According to dual coding theory [99], using text and graphics together to convey information is more effective than using either on their own. When information is presented both verbally and visually, representations of that information are encoded in separate systems in working memory and referential connections between the two are strengthened.

This suggests that textual encoding is most effective when it is used in a supporting role: to supplement rather than to substitute for graphics. In particularly, text should never be used as the sole basis for distinguishing between symbols (as discussed in Perceptual Discriminability) but can be usefully used as a form of redundant coding, to reinforce and clarify meaning. Another argument for dual coding is that people differ widely in their spatial and verbal processing abilities. Including graphics and text is likely to improve understanding by people across the full spectrum of spatial and verbal abilities [143].

**Annotations**

Including textual explanations (annotations) can improve understanding of diagrams in the same way that comments can improve understanding of programs. According to the principle of spatial contiguity [80], including these on the diagram itself is much more effective than including them separately (e.g. in a separate document, as is commonly done in practice). An example of design excellence here is UML, which explicitly includes an annotation construct, though representing it using a graphical symbol was not a good representational choice (as discussed in Semiotic Clarity).

**Hybrid (Graphics+Text) Symbols**

Textual encoding can be used to reinforce and expand the meaning of graphical symbols. The rightmost representation in Figure 32 shows a hybrid (graphics+text) representation of the same relationship shown in Figure 31. This combines the semantic expressiveness of the UML convention with the visual expressiveness of the Oracle convention, while also taking advantage of dual coding.

![Figure 32. Dual Coding: the Best of Both Worlds?](image)

In the hybrid representation, the text both expands and reinforces the meaning of the graphics:

- It expands its meaning by enabling exact minimum and maximum cardinalities to be specified.
- It reinforces its meaning by providing an additional cue to what it means. Empirical studies show that novices sometimes have difficulty remembering what cardinality symbols
mean on ER diagrams [35, 52]: redundantly including textual cardinalities increases the likelihood they will be accurately interpreted. The text thus adds value even if the cardinalities are all 0, 1, or many.

Dual coding does not affect discriminability as visual distance is not affected by the addition of text. However, it aids interpretation by providing textual cues to the meaning of symbols when they are not semantically transparent and improves retention through interlinked visual and verbal encoding in memory.

4.8 Principle of Graphic Economy: The number of different graphical symbols should be cognitively manageable

Graphic complexity is defined by the number of graphical symbols in a notation: the size of its visual vocabulary [93]. This differs from diagrammatic complexity (Complexity Management), as it relates to complexity at the type (language) level rather than the token (sentence) level. A notation designer can create an unlimited number of symbols by combining visual variables together in different ways. However, compared to textual languages, this strategy is only effective up to a certain point, as there are cognitive limits on the number of visual categories that can be effectively recognised [138]. Beyond this, each new symbol introduced reduces cognitive effectiveness.

Graphic complexity affects novices much more than experts, as they need to consciously maintain meanings of symbols in working memory. If the symbols are not mnemonic, the user must remember what the symbols mean or else a legend must be supplied and frequently referenced, which all adds to the effort of processing diagrams. Empirical studies show that graphic complexity significantly reduces understanding of SE diagrams by novices [93].

The human ability to discriminate between perceptually distinct alternatives (span of absolute judgement) is around 6 categories [82]: this defines an upper limit for graphic complexity. Many SE notations exceed this limit by an order of magnitude: for example, UML Class Diagrams have a graphic complexity of over 40. Interestingly, the two most commonly used notations in practice (DFDs and ER) do satisfy this principle, which may partly explain their longevity and continued popularity in practice.

SE notations tend to increase inexorably in graphic complexity over time, primarily due to efforts to increase their semantic expressiveness. Each new construct normally requires a new symbol and while new constructs are often added, old ones are rarely removed. For example, the first SE notation (program flowcharts) started off with 5 symbols [36] but expanded by a factor of 8 by the time the final ISO standard was published [58]. There are three main strategies for dealing with excessive graphic complexity:

- Reduce semantic complexity
- Introduce symbol deficit
- Increase visual expressiveness

Reduce (or partition) semantic complexity

The number of semantic constructs in a notation is a major determinant of graphic complexity as different constructs are usually represented by different symbols. Simplifying the semantics of a notation thus provides an obvious way of reducing graphic complexity. In more complex languages (e.g. UML, ArchiMate), the semantic constructs may need to be partitioned to reduce graphic and diagrammatic complexity.

Introduce symbol deficit

Graphic complexity can also be reduced directly (without affecting semantics) by introducing symbol deficit (Semiotic Clarity). This means choosing not to show some constructs graphically. This changes the balance between graphical and textual encoding in the notation, as the constructs removed from the visual notation will usually need to be defined in text. Most visual notations rely at least to some extent on text to keep their visual vocabularies manageable: it is the general purpose tool of last resort [96]. The interpretation of any SE diagram almost always depends on a division of labour between graphics and text [44, 96]. Where this line is drawn (the graphics-text boundary) is a critical design decision. Another important design decision is how much information to include on the diagram itself and how much in supporting definitions (ondiagram vs off-diagram).

![Figure 33. A Balancing Act: to keep graphic (and diagram) complexity manageable, notation designers need to make decisions about what information to encode graphically, what to encode textually and what to include in supporting definitions.](image_url)

Diagrams work best as abstractions or summaries rather than standalone specifications and showing too much information graphically can be counterproductive [44, 96]. Also, some information is more effectively encoded in textual form: diagrams are better for representing some types of information but worse for others (e.g. business rules, detailed procedural logic) [44]. Part of the secret to using visual notation effectively may be knowing when not to use it [22, 103]: to find the right balance between graphical, textual and off-diagram encoding that maximises computational offloading while avoiding excessive graphic and diagrammatic complexity (Figure 33).

Many SE notations make the mistake of trying to encode too much information in graphical form. For example, ORM uses 21 different graphical symbols to represent different types of constraints [49], even though graphics is poorly suited for encoding such information (as shown by the largely unsuccessful attempts to develop visual notations for modelling business rules [e.g. 112]).

Increase visual expressiveness

This is an approach to dealing with excessive graphic complexity that works not by reducing the number of symbols but by increasing human discrimination ability. The span of absolute judgement can be expanded by increasing the number of perceptual dimensions on which stimuli differ [82]. The 6 symbol...
limit thus only applies if a single visual variable is used (which is true for most SE notations, which use shape as the sole information-carrying variable). Using multiple visual variables to differentiate between symbols (Visual Expressiveness) can increase human discrimination ability in an almost additive manner. Figure 29 shows how multiple visual variables can be used to effectively distinguish between a large number of categories.

4.9 Principle of Cognitive Fit: Use different visual dialects for different tasks and audiences

Cognitive fit theory is a widely accepted theory in the information systems (IS) field that has been validated in a wide range of domains, from managerial decision making to program maintenance [116, 136, 137]. The theory states that different representations of information are suitable for different tasks and different audiences. Problem solving performance (which corresponds roughly to cognitive effectiveness) is determined by a three-way fit between the problem representation, task characteristics and problem solver skills (Figure 34).

![Figure 34. Cognitive fit is the result of a three-way interaction between the representation, task and problem solver [136]](image)

Most SE notations exhibit visual monolingualism: they use a single visual representation for all purposes. However, cognitive fit theory suggests that this “one size fits all” assumption may be inappropriate and that different visual dialects may be required for different tasks and/or audiences (“representational horses for cognitive courses” [103]). These represent complementary rather than competing visual dialects as discussed earlier. There are at least two reasons for creating multiple visual dialects in an SE context:

- Expert-novice differences (problem solver skills)
- Representational medium (task characteristics)

Expert-novice differences

One of the major challenges in designing SE notations is the need to develop representations that are understandable by both business and technical experts. This adds to the difficulty of the task as in most engineering contexts, diagrams are only used to communicate among experts. There are well-known differences in the way experts and novices process diagrams [21, 62, 73, 95, 135, 148]. While we all have the same perceptual and cognitive hardware, notation experts develop diagram schemas in long term memory which largely automate the process of diagram interpretation [19, 104]. For non-experts, interpretation is slower, more error-prone and requires conscious effort. The most important expert-novice differences are:

- Novices have more difficulty discriminating between symbols [15, 62]
- Novices have to consciously remember what symbols mean [148]
- Novices are more affected by complexity, as they lack “chunking” strategies [12]

These differences are rarely taken into account in the design of SE visual notations, even though they are routinely used to communicate with business stakeholders (who are domain experts but notational novices). While it might seem reasonable to design a notation to be understandable to novices and use this also for experts (following the “least common denominator” principle), cognitive load theory (not related to cognitive fit theory) suggests this may be incorrect. Optimising representations for novices can reduce their effectiveness for experts and vice versa: this is called the expertise reversal effect [59].

The well-documented differences between experts and novices suggest the need for at least two different visual dialects: an expert (“pro”) and a novice (“lite”) one. Notations designed for communication with novices will need to use more discriminable symbols (Perceptual Discriminability), reduced complexity (Complexity Management), more mnemonic conventions (Semantic Transparency), explanatory text (Dual Coding) and simplified visual vocabularies (Graphic Economy).

Practitioners sometimes develop their own, informal notations for communicating with users (usually simplified versions of the standard notation), but this capability should be provided by the primary notation rather than leaving it to secondary notation. Two examples of design excellence in this regard are ORM [49] and Oracle data modelling [6], which define specialised notations for communicating with end users. ORM uses a tabular representation while Oracle defines a natural language based normative language [53] (which supports Dual Coding).

Representational medium

Another situation that may require different visual dialects is different representational media. In particular, requirements for sketching on whiteboards or paper (an important use of visual notations in early design stages), are different to those for using computer-based drawing tools (Figure 35). Hand drawing presents special challenges for visual notation design because of the limited drawing abilities of software engineers (as drawing is typically not a skill included in SE curricula). Some of the most important differences are:

- Perceptual Discriminability: discriminability requirements are higher due to variations in how symbols are drawn by different people. As within-symbol variations increase, between-symbol differences need to be more pronounced.
- Semantic Transparency: pictures and icons are more difficult to draw than simple geometric shapes, especially for the artistically challenged.
- Visual Expressiveness: some visual variables (colour, value and texture) are more difficult to use (due to limited drawing ability and availability of equipment e.g. colour pens).

The need to use notations for sketching provides a possible explanation for why SE visual notations have such limited visual vocabularies. Requirements for hand drawing may have acted to constrain their visual expressiveness, and would explain why highly effective techniques such as colour, icons and 3D shapes are so rarely used. In fact, most SE visual notations seem designed for the pre-computer era, as they make little use of the powerful capabilities of modern graphics software: effec-
tively they are designed for pencil-and-paper. Cognitive fit allows the best of both worlds: a simplified visual dialect for sketching and an enriched notation for final diagrams.

Semantic Transparency and Visual Expressiveness can make hand drawing more difficult (Cognitive Fit).

### 5. Conclusion

Historically, issues of visual syntax have been ignored or undervalued in SE research. One aim of this paper is to raise awareness about the importance of such issues in notation design. Visual representation decisions have a profound effect on the usability and effectiveness of SE notations, equal to (if not greater than) decisions about semantics. For this reason, visual syntax deserves at least equal effort and attention in the notation design process.

Visual notation design currently exists as a “dark art”, an unconscious process that resists explanation even by those who practise it [53]. The goal of this paper is to establish the foundations for a science of visual notation design: to help it progress from a craft to a design discipline (self-conscious process) based on explicit principles. Having sound principles for designing visual syntax (distinct from those for designing semantics) will enable notation designers to design both syntax and semantics of notations in a systematic manner. It will also help them to clearly separate syntactic and semantic issues, which are frequently confused: this supports separation of concerns, one of the basic tenets of SE.

SE visual notations are currently designed without explicit design rationale. In the same way that reasons for design decisions should be provided when designing software systems, they should also be provided when designing visual notations. We need to be able to defend our graphic designs and provide sound justification for visual representation choices [132]. Ideally, such justifications should be based on scientific evidence rather than subjective criteria, as is currently the case.

A surprising result of our analysis of existing SE notations is that some older (even obsolete) visual notations such as DFDs are better designed than more recent ones, contrary to expectations of “notational Darwinism”. Without sound principles for visual notation design, practice can just as easily go backwards as forwards (like any unconscious culture). Naïve theories of graphic design (like naïve theories of physics [81] or psychology [94]) are as likely to be wrong as they are to be right.

### 5.1 The Physics of Notations: A Theory for Visual Notation Design

The Physics of Notations consists of three key components: a design goal, a descriptive theory and a prescriptive theory:

**The Dependent Variable (Design Goal)**

Cognitive effectiveness is defined as the primary dependent variable for evaluating and comparing visual notations and the primary design goal in constructing them. This variable is operationally defined and can therefore be empirically evaluated.

**Descriptive (Type IV) Theory: How Visual Notations Communicate**

Section 3 defines a theory of how and why visual notations communicate, based on extant theories from communication, semiotics, graphic design, visual perception and cognition. This provides a basis for explaining and predicting why some visual representations will be more effective than others.
Prescriptive (Type V) Theory: Principles for Designing Cognitively Effective Visual Notations

Section 4 defines a set of principles for designing cognitively effective visual notations. These provide a scientific basis for comparing, evaluating, improving, and constructing visual notations, which has previously been lacking in the SE field. Importantly, these principles are not based on common sense, experience or observations of “best practices” but on theory and empirical evidence about cognitive effectiveness of visual representations. They synthesise the best available research evidence from a wide range of fields, including communication, semiotics, graphic design, visual perception, psychophysics, cognitive psychology, HCI, information visualisation, information systems, education, cartography and diagrammatic reasoning.

Together, the principles form a design (Type V) theory. Gregor and Jones [46] have defined a template for specifying such theories: Table 3 shows how the Physics of Notations fits into this. All components are specified except mutability of artifacts (which relates to evolution of notations), which suggests a possible direction for future research. In comparison, the CDs framework only “ticks” two of the boxes (Constructs and Expository Instantiation), confirming that it is a Type I theory.

<table>
<thead>
<tr>
<th>Component</th>
<th>The Physics of Notations</th>
</tr>
</thead>
<tbody>
<tr>
<td>Scope and Purpose</td>
<td>To design cognitively effective visual notations</td>
</tr>
<tr>
<td>Constructs</td>
<td>Visual notation (language), visual sentence (diagram), visual dialect, visual vocabulary (symbol set), visual grammar (composition rules), graphical symbol (type), symbol instance (token), visual variable, cognitive effectiveness</td>
</tr>
<tr>
<td>Principles of form and function</td>
<td>Semiotic Clarity, Perceptual Discriminability, Semantic Transparency, Complexity Management, Cognitive Integration, Visual Expressiveness, Dual Coding, Graphic Economy, Cognitive Fit (all principles of form)</td>
</tr>
<tr>
<td>Artifact mutability</td>
<td>[Not addressed]</td>
</tr>
<tr>
<td>Testable propositions</td>
<td>Visual notations that satisfy the principles will be more cognitively effective than those that do not. The theory effectively defines a causal model with the principles as independent variables (causes) and cognitive effectiveness as the dependent (outcome) variable.</td>
</tr>
<tr>
<td>Justificatory knowledge</td>
<td>Information theory, graphic design theory, theory of symbols, feature integration theory, object recognition theory, psychophysics theory, semiotic theory, cognitive load theory, cognitive integration theory, working memory theory, gestalt theory, cognitive fit theory, dual coding theory, schema theory, human information processing theory, multimedia learning theory, wayfinding theory, cartographic abstraction theory, modularity theory, ontological theory</td>
</tr>
<tr>
<td>Principles of implementation (optional)</td>
<td>Methods for evaluating notations (e.g. perceptual popout analysis for evaluating Perceptual Discriminability)</td>
</tr>
<tr>
<td>Expository instantiation (optional)</td>
<td>Methods for improving notations (e.g. redundant coding for improving PD).</td>
</tr>
<tr>
<td>Expository examples: UML, ER, DFDs, ArchiMate, EPCs, ORM, rich pictures, program flowcharts, cartography.</td>
<td></td>
</tr>
</tbody>
</table>

Gregor and Jones’s template is an important contribution for two reasons:

- It recognises design theories as a separate and legitimate class of scientific theories. This is important for researchers in artificial sciences (like SE), where they represent the majority of theories proposed [34].
- It helps clarify and formalise the structure of design theories. Design (artificial science) theories are fundamentally different to traditional (natural science) theories, but are typically presented in a wide variety of formats.

5.2 Practical Significance

A significant proportion of SE research and practice is devoted to method engineering. In most cases, visual notations form an integral part of the methods proposed. The principles in this paper can be used by notation designers to:

- Design notations: visual notations can be constructed in a systematic way, based on the semantics to be expressed. Existing SE notations use a limited variety of visual forms, a well-known characteristic of unselfconscious design cultures [1]. Having explicit design principles supports more extensive exploration of the design space and development of new and innovative visual forms.
- Compare notations: the principles support comparison of notations, where syntactic and semantic issues are often confused. They also provide the basis for resolving some longstanding disputes about the relative merits of competing visual dialects (e.g. De Marco vs Gane & Sarson DFDs, IE vs Chen ER diagrams)\(^9\).
- Evaluate and improve notations: the principles can be used to identify potential problems in existing visual notations and to resolve them. This paper has identified serious design flaws in some of the leading SE notations, together with some suggestions for how they could be improved: however these represent only the “tip of the iceberg” of improvements that are possible (e.g. see [85, 87, 89]).

Impact on SE Practice

A major focus in this paper has been on improving understanding of visual notations by business stakeholders (end users and customers). This is particularly important in an SE context, as effective user-developer communication is critical for successful development of software systems. It is also one of the major weaknesses in existing SE notations: expert-novice differences are rarely taken into account in their design, even though they are routinely used to communicate with novices.

However, visual notations are also used for communication among technical experts (e.g. members of the development team) and as cognitive externalisations [150] to support design and problem solving. Improving their cognitive effectiveness will also improve their utility for these purpose: optimising visual notations for human information processing will optimise them for use by both software engineers and their customers, who share the same perceptual and cognitive hardware and software (subject to considerations of Cognitive Fit).

\(^9\) Space does not permit a full analysis here, but De Marco DFDs should be preferred on grounds of Perceptual Discriminability and Visual Expressiveness while IE ER diagrams should be preferred based on Perceptual Discriminability, Semantic Transparency, and Visual Expressiveness.
The principles defined in this paper represent an initial starting point for establishing a science of visual notation design. However, further research is required to test, refine and extend the principles.

Validation of Principles: Truth vs Utility

The principles proposed in this paper are based on principles of visual perception and cognition (Section 3) and a Type V theory (Section 4), which are higher evolutionary forms than the CDs framework (Type I). However, it should not be seen as a direct competitor for the CDs framework as its scope is much more modest (visual notations rather than cognitive artifacts). Instead, it should be seen as complementary: it provides exactly the type of detailed, domain-specific analysis that the authors of the CDs framework argued was necessary to supplement the “broad brush” analysis provided by CDs [44]. It also focuses exclusively on visual representation aspects, which the CDs framework excludes.

5.4 Limitations and Further Research

Encoding side design goals

This paper defines cognitive effectiveness as the primary goal in visual notation design. This is a decoding-side (processing) goal: effectiveness is defined from the receiver’s rather than the sender’s viewpoint (cf. Figure 6). However, ease of expression, an encoding-side goal, is also an important consideration in design of visual notations: for example, one of the barriers to the adoption of UML is that many programmers find it easier to write code directly than produce UML diagrams first. Encoding-side and decoding-side goals can often be in conflict, like the R-principle (minimising speaker’s effort) and Q-principle (minimising listener’s effort) in linguistics [55]. The Physics of Notations does not consider encoding-side issues as it focuses only on the effectiveness of the resulting representation. Further research could expand the theory to include such considerations.

5.5 Wider Significance

The principles defined in this paper also provide a potential contribution outside the SE field. Visual notations are used in a wide range of scientific fields e.g. physics (Feynman diagrams), biology (cladograms), chemistry (molecular structure diagrams), mathematics (Venn diagrams), education (knowledge maps), engineering (circuit diagrams), linguistics (parse trees) and scientific research (causal graphs). While the principles were specifically developed for designing SE notations, they are based on general principles of visual perception and cognition so in principle are applicable to visual notations in any domain.
6. REFERENCES


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